

CLAIMS

1. a countermeasure method for implementation in  
an electronic component implementing a public-key  
5 cryptography algorithm comprising exponentiation  
computation, with a left-to-right type exponentiation  
algorithm, of the type  $y=g^d$ , where g and y are  
elements of the determined group G written in  
multiplicative notation, and d is a predetermined  
10 number, said countermeasure method being characterized  
in that it includes a random draw step, at the start of  
or during execution of said exponentiation algorithm in  
deterministic or in probabilistic manner, so as to mask  
the accumulator A.

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2. A countermeasure method according to claim 1,  
characterized in that the group G is written in  
additive notation.

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3. A countermeasure method according to claim 1,  
characterized in that the group G is the multiplicative  
group of a finite field written  $GF(q^n)$ , where n is an  
integer.

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4. A countermeasure method according to claim 3,  
characterized in that the integer is n equal to 1: n=1.

5. A countermeasure method according to claim 4,  
characterized in that it comprises the following steps:

- 1) Determine an integer  $k$  defining the security of the masking and give  $d$  by the binary representation  $(d(t), d(t-1), \dots, d(0))$
- 2) Initialize the accumulator  $A$  with the integer 1
- 5 3) For  $i$  from  $t$  down to 0, do the following:
  - 3a) Draw a random integer  $\lambda$  lying in the range 0 to  $k-1$  and replace the accumulator  $A$  with  $A+\lambda.q$  (modulo  $k.q$ )
  - 10 3b) Replace  $A$  with  $A^2$  (modulo  $k.q$ )
  - 3c) If  $d(i)=1$ , replace  $A$  with  $A.g$  (modulo  $k.q$ )
- 4) Return  $A$  (modulo  $q$ ).

15 6. A countermeasure method according to claim 4, characterized in that it comprises the following steps:

- 1) Determine an integer  $k$  defining the security of the masking, and give  $d$  by the binary representation  $(d(t), d(t-1), \dots, d(0))$
- 20 2) Draw a random integer  $\lambda$  lying in the range 0 to  $k-1$  and initialize the accumulator  $A$  with the integer  $1+\lambda.q$  (modulo  $k.q$ )
- 3) For  $i$  from  $t-1$  down to 0, do the following:
  - 3a) Replace  $A$  with  $A^2$  (modulo  $k.q$ )
  - 25 3b) If  $d(i)=1$ , replace  $A$  with  $A.g$  (modulo  $k.q$ )
- 4) Return  $A$  (modulo  $q$ ).

7. A countermeasure method according to claim 2, characterized in that the exponentiation algorithm applies to the group G of the points of an elliptic curve defined on the finite field  $GF(q^n)$ .

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8. A countermeasure method according to claim 7, characterized in that it comprises the following steps:

- 1) Initialize the accumulator  $A = (A_x, A_y, A_z)$  with the  $(x, y, 1)$  triplet and give d by the binary signed-digit representation  $(d(t+1), d(t), \dots, d(0))$  with  $d(t+1)=1$
- 2) For i from t down to 0, do the following:
  - 2a) Draw a random non-zero element  $\lambda$  from  $GF(q^n)$  and replace the accumulator  $A = (A_x, A_y, A_z)$  with  $(\lambda^2 \cdot A_x, \lambda^3 \cdot A_y, \lambda \cdot A_z)$
  - 2b) Replace  $A = (A_x, A_y, A_z)$  with  $2 \cdot A = (A_x, A_y, A_z)$  in Jacobian representation, on the elliptic curve
  - 2c) If  $d(i)$  is non-zero, replace  $A = (A_x, A_y, A_z)$  with  $(A_x, A_y, A_z) + d(i) * (x, y, 1)$  in Jacobian representation on the elliptic curve
- 3) If  $A_z=0$ , return the point at infinity; otherwise return  $(A_x / (A_z)^2, A_y / (A_z)^3)$ .

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9. A countermeasure method according to claim 7, characterized in that it comprises the following steps:

- 1) Draw a non-zero random element  $\lambda$  from  $GF(q^n)$  and initialize the accumulator  $A = (A_x, A_y, A_z)$  with the  $(\lambda^2 \cdot x, \lambda^3 \cdot y, \lambda)$  triplet and give d by

the binary signed-digit representation  $(d(t+1), d(t), \dots, d(0))$  with  $d(t+1)=1$

2) For  $i$  from  $t$  down to 0, do the following:

5      2a) Replace  $A=(A_x, A_y, A_z)$  with  $2*A=(A_x, A_y, A_z)$  in Jacobian representation, on the elliptic curve

2b) If  $d(i)$  is non-zero, replace  $A=(A_x, A_y, A_z)$  with  $(A_x, A_y, A_z) + d(i) * (x, y, 1)$  in Jacobian representation on the elliptic curve

10     3) If  $A_z=0$ , return the point at infinity; otherwise return  $(A_x / (A_z)^2, A_y / (A_z)^3)$ .

10. A countermeasure method according to claim 7, characterized in that it comprises the following steps:

15     1) Initialize the accumulator  $A=(A_x, A_y, A_z)$  with the  $(x, y, 1)$  triplet and give  $d$  by the binary signed-digit representation  $(d(t+1), d(t), \dots, d(0))$  with  $d(t+1)=1$

2) For  $i$  from  $t$  down to 0, do the following:

20     2a) Draw a random non-zero element  $\lambda$  from  $GF(q^n)$  and replace the accumulator  $A=(A_x, A_y, A_z)$  with  $(\lambda \cdot A_x, \lambda \cdot A_y, \lambda \cdot A_z)$

2b) Replace  $A=(A_x, A_y, A_z)$  with  $2*A=(A_x, A_y, A_z)$  in homogeneous representation, on the elliptic curve

25     2c) If  $d(i)$  is non-zero, replace  $A=(A_x, A_y, A_z)$  with  $(A_x, A_y, A_z) + d(i) * (x, y, 1)$  in homogeneous representation on the elliptic curve

3) If  $A_z=0$ , return the point at infinity;  
 otherwise return  $(A_x/A_z, A_y/A_z)$ .

11. A countermeasure method according to claim 7,  
 5 characterized in that it comprises the following steps:

- 1) Draw a non-zero random element  $\lambda$  from  $GF(q^n)$   
 and initialize the accumulator  $A=(A_x, A_y, A_z)$   
 with the  $(\lambda.x, \lambda.y, \lambda)$  triplet and give  $d$  by the  
 binary signed-digit representation  $(d(t+1),$   
 10  $d(t), \dots, d(0))$  with  $d(t+1)=1$
- 2) For  $i$  from  $t$  down to 0, do the following:
  - 2a) Replace  $A=(A_x, A_y, A_z)$  with  $2*A=(A_x, A_y, A_z)$   
 in homogeneous representation, on the  
 elliptic curve
  - 2b) If  $d(i)$  is non-zero, replace  $A=(A_x, A_y, A_z)$   
 with  $(A_x, A_y, A_z) + d(i) * (x, y, 1)$  in  
 homogeneous representation on the  
 elliptic curve
- 3) If  $A_z=0$ , return the point at infinity;  
 20 otherwise return  $(A_x/A_z, A_y/A_z)$ .

12. An electronic component using the  
 countermeasure method according to any preceding claim.